Advanced CS #1: Data Representation

CS SCHOLARS – PROGRAMMING

Learning Objectives

- Understand how different **number systems** can represent the same information

- Translate **binary numbers** to decimal, and vice versa

- Interpret binary numbers as abstracted types, including **colors** and **text**

Number Systems

Computers Run on 0s and 1s

Computers represent everything by using 0s and 1s. You've likely seen references to this before.

How can we represent text, or images, or sound with 0s and 1s? This brings us back to **abstraction**.
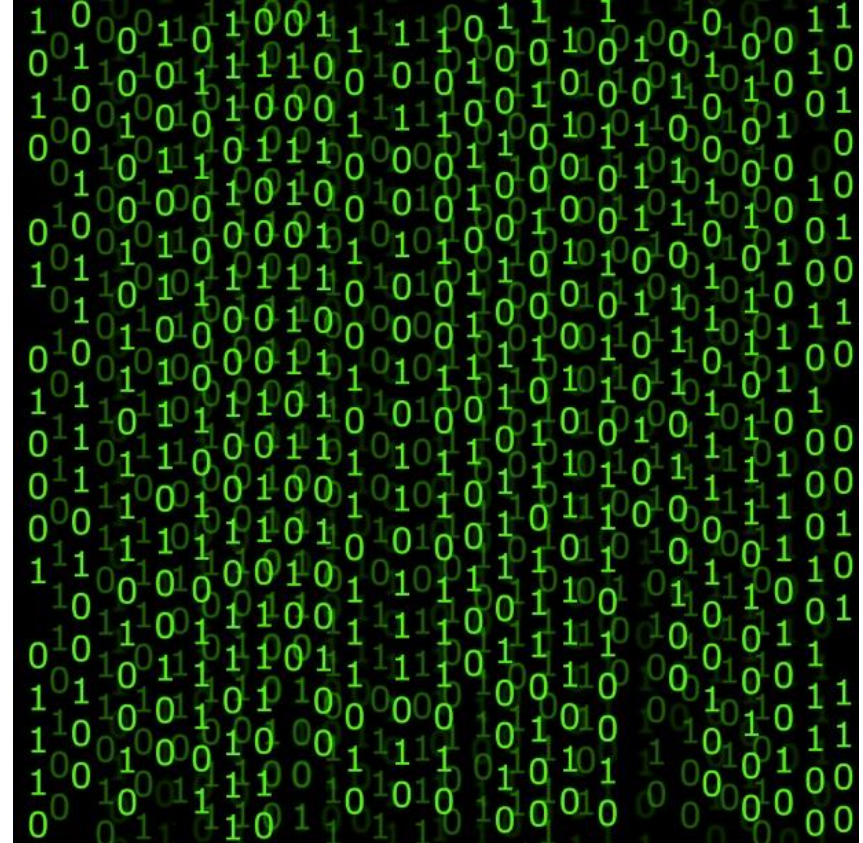
Abstraction is About Representation

Recall our definition of abstraction from the first lecture:

Abstraction is a technique used to make complex systems manageable by changing the amount of detail used to **represent** or interact with the system.

We'll use abstraction to translate 0s and 1s to decimal numbers, then translate those numbers to other types.

Number Systems – Coins

A **number system** is a way of representing numbers using symbols.

One example of a number system is US currency. How much is each of the following symbols worth?
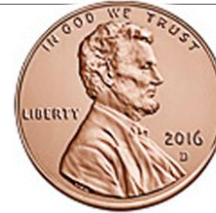
Penny
1 cent

Nickel
5 cents

Dime
10 cents

Quarter
25 cents

Number Systems – Dollars

Alternatively, we can represent money using **dollars and cents**, in decimal form.

For example, a medium coffee at Tazza D'oro, the campus coffee shop, is **$2.65**.

Converting Coins to Dollars

We can **convert between number systems** by translating a value from one system to the other.

For example, the coins on the left represent the same value as $0.87

Using pictures is clunky. Let's make a new representation system for coins.

Coin Number Representation

To represent coins, we'll make a number with four digits.

The first represents quarters, the second dimes, the third nickels, and the fourth pennies.

c.3.1.0.2 =

3*$0.25 + 1*$0.10 + 0*$0.05 + 2*$0.01 =

$0.87

	Q	D	N	P
c	3	1	0	2

Converting Dollars to Coins

What if we want to go in the opposite direction? What if you want to convert dollars to coins?

Start by picking the largest coin (a quarter). Remove as many quarters from the dollar amount as you can.

Then repeat with the next-largest coin (dime), and so on (nickel), until you reach the smallest coin (penny).

Example: What is $0.59 in coin representation?

$0.59 = 2*$0.25 + 0*$0.10 + 1*$0.05 + 4*$0.01 = c.2.0.1.4

Activity: Coin Conversion

Now try the following calculations:

What is c.1.1.1.2 in dollars?

What is $0.61 in coin representation?

Activity Answers

What is c.1.1.1.2 in dollars?

$0.42

What is $0.61 in coin representation?

c.2.1.0.1

Number Systems – Binary

Now let's go back to computers. We can represent numbers using only 0s and 1s with the **binary number system**.

Instead of counting the number of 1s, 5s, 10s, and 25s in coins you need, count the number of 1s, 2s, 4s, and 8s.

Why these numbers? They're **powers of 2**. This is a number in **base 2,** which only needs the digits 0 and 1. In contrast, our usual decimal system uses base 10 (with digits 0-9).

2^3 8	2^2 4	2^1 2	2^0 1
1	1	0	1

Bits and Bytes

When working with binary and computers, we often refer to a set of binary values used together to represent a number.

A single binary value is called a **bit**.

A set of 8 bits is called a **byte**.

We commonly use some number of **bytes** to represent data values.

Counting in Binary

0 =

128	64	32	16	8	4	2	1
0	0	0	0	0	0	0	0

1 =

128	64	32	16	8	4	2	1
0	0	0	0	0	0	0	1

2 =

128	64	32	16	8	4	2	1
0	0	0	0	0	0	1	0

3 =

128	64	32	16	8	4	2	1
0	0	0	0	0	0	1	1

4 =

128	64	32	16	8	4	2	1
0	0	0	0	0	1	0	0

5 =

128	64	32	16	8	4	2	1
0	0	0	0	0	1	0	1

6 =

128	64	32	16	8	4	2	1
0	0	0	0	0	1	1	0

7 =

128	64	32	16	8	4	2	1
0	0	0	0	0	1	1	1

Converting Binary to Decimal

To convert a binary number to decimal, just add each power of 2 that is represented by a 1.

For example, 00011000 = 16 + 8 = 24

128	64	32	16	8	4	2	1
0	0	0	1	1	0	0	0

Another example:

10010001 = 128 + 16 + 1 = 145

128	64	32	16	8	4	2	1
1	0	0	1	0	0	0	1

Converting Decimal to Binary

Converting decimal to binary uses the **same process** as converting dollars to coins.

Look for the largest power of 2 that can fit in the number and subtract it from the number. Repeat with the next power of 2, etc., until you reach 0.

For example, 36 = 32 + 4 = 00100100

128	64	32	16	8	4	2	1
0	0	1	0	0	1	0	0

Another example:

103 = 64 + 32 + 4 + 2 + 1

128	64	32	16	8	4	2	1
0	1	1	0	0	1	1	1

Activity: Converting Binary

Now try converting numbers on your own.

First: what is **01011011** in decimal?

Second: what is **75** in binary?

Activity Answers

First: what is **01011011** in decimal?

64+16+8+2+1 = 91

Second: what is **75** in binary?

 64+8+2+1 = 01001011

Abstracted Types

Binary and Abstraction

Now that we can represent numbers using binary, we can represent **everything** computers store using binary.

We just need to use **abstraction** to interpret bits or numbers in particular ways.

Let's consider numbers, images, and text.

You Do: Representing Negative Numbers

It can be helpful to think logically about how to represent a value before learning how it's done in practice. Let's do that now.

We can convert binary directly into positive numbers, but how do we represent negative numbers?

Take a moment to think about how *you* would represent negative numbers.

Answer: Representing Negative Numbers

Simple Approach: reserve one bit to represent whether the number is positive or negative. Convert the rest normally.

Actual Approach: mathematically, X + (-X) = 0. Set up the binary so that when it is added to the binary of the positive version of the number, the result is 0. Do this by **restricting the number of bits** that will be considered to a preset amount (perhaps 8).

The value 11111111 is 255, but it is also -1 because 11111111 + 1 = 100000000, which becomes 00000000 if we only have 8 bits. 11111110 is -2 (or 254), and so on.

How do we decide whether 11111111 is 255 or -1? It all depends on our **interpretation**. Is the integer signed (possibly negative) or unsigned (definitely positive)?

Size of Integers

Your machine is either classified as 32-bit or 64-bit. This refers to the **size of integers** used by your computer's operating system.

The largest signed integer that can be represented with N bits is 2^N-1 (why?). This means that...

Largest int for 32 bits: 4,294,967,295 (or 2,147,483,647 with negative numbers)

Largest int for 64 bits: 18,446,744,073,709,551,615 (18.4 quintillion)

Integer Overflow

Why does this matter?

By late 2014, the music video Gangnam Style received more than **2 billion** views. When it passed the largest positive number that could be represented with 32 bits, YouTube showed the number of views as **negative** instead!

Now YouTube uses a 64-bit counter instead.
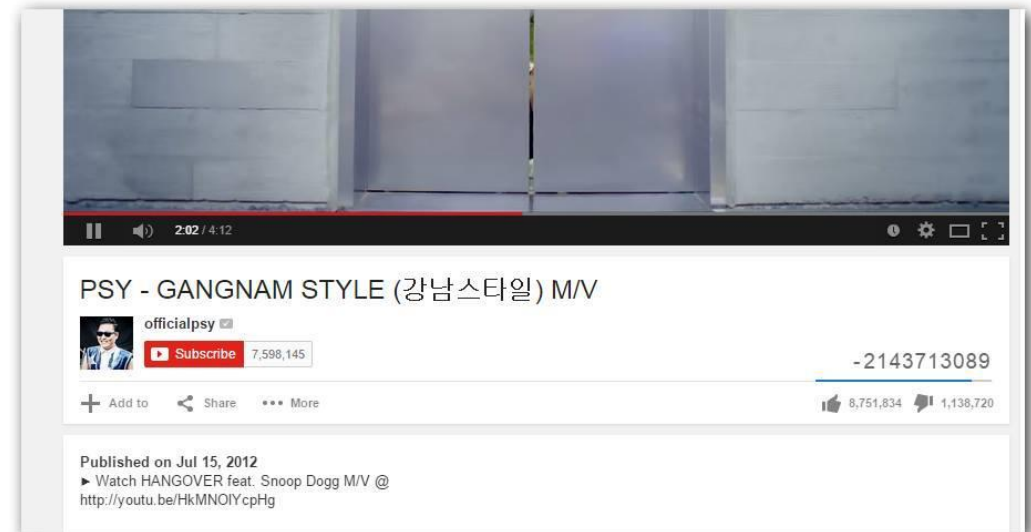
Represent Images as Grids of Colors

What if we want to represent an image? How can we convert that to numbers?

First, break the image down into a grid of colors, where each square of color has a distinct hue. A square of color in this context is called a **pixel**.

If we can represent a pixel in binary, we can interpret a series of pixels as an image.
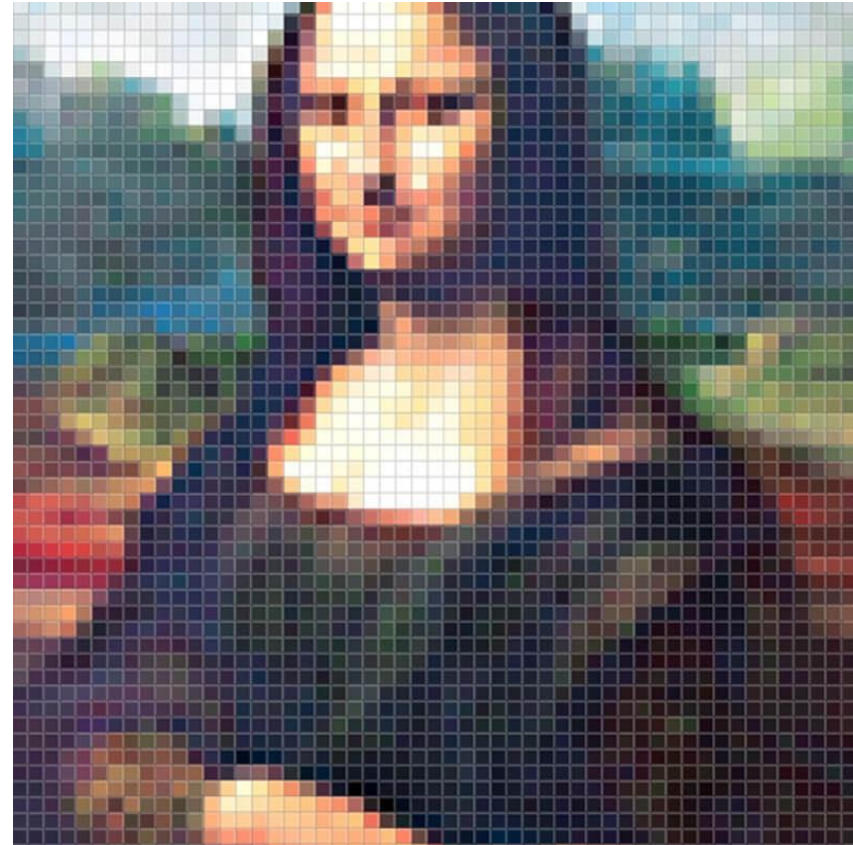
Representing Colors in Binary

We need to represent a single color (a pixel) as a number.

There are a few ways to do this, but we'll focus on **RGB**. Any color can be represented as a combination of Red, Green, and Blue.

Red, green, and blue intensity can be represented using one **byte** each, where 00000000 (0) is none and 11111111 (255) is very intense. Each pixel will therefore require 3 bytes to encode.

Try it out here:
w3schools.com/colors/colors_rgb.asp
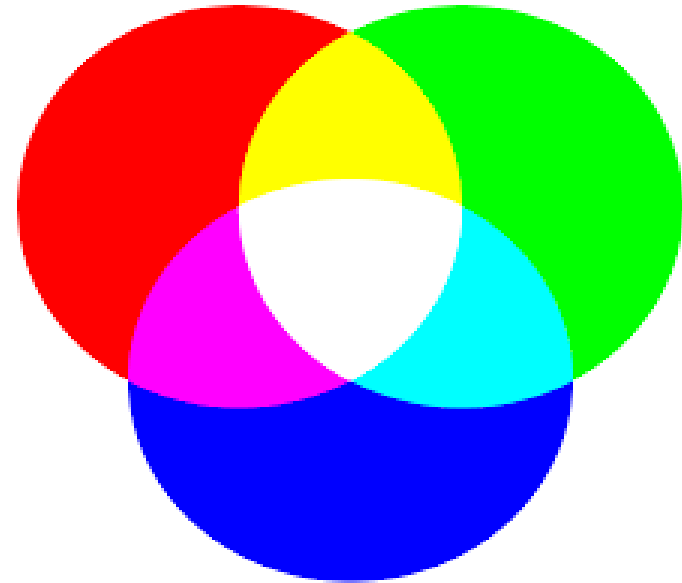
Example: Representing Beige

To make the campus-building beige, we'd need:

Red   = 249 = 11111001

Green = 228 = 11100100

Blue   = 183 = 10110111

Which makes beige!

Represent Text as Individual Characters

Next, how do we represent text?

First, we break it down into smaller parts, like with images. In this case, we can break text down into individual **characters**.

For example, the text "Hello World" becomes

H, e, l, l, o, space, W, o, r, l, d

Use a Lookup Table to Convert Characters

Unlike colors, characters don't have a natural connection to numbers.

Instead, we can use a **lookup table** that maps each possible character to an integer.

As long as every computer uses the same lookup table, computers can always translate a set of numbers into the same set of characters.

ASCII is a Simple Lookup Table

For basic characters, we can use the encoding system called ASCII. This maps the numbers 0 to 255 to characters. Therefore, one character is represented by one byte.

Check it out here:
www.asciitable.com

Dec	Hex	Oct	Chr	Dec	Hex	Oct	HTML	Chr	Dec	Hex	Oct	HTML	Chr	Dec	Hex	Oct	HTML	Chr
0	0	000	NULL	32	20	040	 	Space	64	40	100	@	@	96	60	140	`	`
1	1	001	Start of Header	33	21	041	!	!	65	41	101	A	A	97	61	141	a	a
2	2	002	Start of Text	34	22	042	"	"	66	42	102	B	B	98	62	142	b	b
3	3	003	End of Text	35	23	043	#	#	67	43	103	C	C	99	63	143	c	c
4	4	004	End of Transmission	36	24	044	$	$	68	44	104	D	D	100	64	144	d	d
5	5	005	Enquiry	37	25	045	%	%	69	45	105	E	E	101	65	145	e	e
6	6	006	Acknowledgment	38	26	046	&	&	70	46	106	F	F	102	66	146	f	f
7	7	007	Bell	39	27	047	'	'	71	47	107	G	G	103	67	147	g	g
8	8	010	Backspace	40	28	050	(	(	72	48	110	H	H	104	68	150	h	h
9	9	011	Horizontal Tab	41	29	051	)	)	73	49	111	I	I	105	69	151	i	i
10	A	012	Line feed	42	2A	052	*	*	74	4A	112	J	J	106	6A	152	j	j
11	B	013	Vertical Tab	43	2B	053	+	+	75	4B	113	K	K	107	6B	153	k	k
12	C	014	Form feed	44	2C	054	,	,	76	4C	114	L	L	108	6C	154	l	l
13	D	015	Carriage return	45	2D	055	-	-	77	4D	115	M	M	109	6D	155	m	m
14	E	016	Shift Out	46	2E	056	.	.	78	4E	116	N	N	110	6E	156	n	n
15	F	017	Shift In	47	2F	057	/	/	79	4F	117	O	O	111	6F	157	o	o
16	10	020	Data Link Escape	48	30	060	0	0	80	50	120	P	P	112	70	160	p	p
17	11	021	Device Control 1	49	31	061	1	1	81	51	121	Q	Q	113	71	161	q	q
18	12	022	Device Control 2	50	32	062	2	2	82	52	122	R	R	114	72	162	r	r
19	13	023	Device Control 3	51	33	063	3	3	83	53	123	S	S	115	73	163	s	s
20	14	024	Device Control 4	52	34	064	4	4	84	54	124	T	T	116	74	164	t	t
21	15	025	Negative Ack.	53	35	065	5	5	85	55	125	U	U	117	75	165	u	u
22	16	026	Synchronous idle	54	36	066	6	6	86	56	126	V	V	118	76	166	v	v
23	17	027	End of Trans. Block	55	37	067	7	7	87	57	127	W	W	119	77	167	w	w
24	18	030	Cancel	56	38	070	8	8	88	58	130	X	X	120	78	170	x	x
25	19	031	End of Medium	57	39	071	9	9	89	59	131	Y	Y	121	79	171	y	y
26	1A	032	Substitute	58	3A	072	:	:	90	5A	132	Z	Z	122	7A	172	z	z
27	1B	033	Escape	59	3B	073	;	;	91	5B	133	[	[	123	7B	173	{	{
28	1C	034	File Separator	60	3C	074	<	<	92	5C	134	\	\	124	7C	174	|	|
29	1D	035	Group Separator	61	3D	075	=	=	93	5D	135	]	]	125	7D	175	}	}
30	1E	036	Record Separator	62	3E	076	>	>	94	5E	136	^	^	126	7E	176	~	~
31	1F	037	Unit Separator	63	3F	077	?	?	95	5F	137	_	_	127	7F	177	&#127;	Del

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Translating Text to Numbers

"Hello World" =

01001000

01100101

01101100

01101100

01101111

00100000

01010111

01101111

01110010

01101100

01100100

Dec	Hex	Oct	Chr
0	0	000	NULL
1	1	001	Start of Header
2	2	002	Start of Text
3	3	003	End of Text
4	4	004	End of Transmission
5	5	005	Enquiry
6	6	006	Acknowledgment
7	7	007	Bell
8	8	010	Backspace
9	9	011	Horizontal Tab
10	A	012	Line feed
11	B	013	Vertical Tab
12	C	014	Form feed
13	D	015	Carriage return
14	E	016	Shift Out
15	F	017	Shift In
16	10	020	Data Link Escape
17	11	021	Device Control 1
18	12	022	Device Control 2
19	13	023	Device Control 3
20	14	024	Device Control 4
21	15	025	Negative Ack.
22	16	026	Synchronous idle
23	17	027	End of Trans. Block
24	18	030	Cancel
25	19	031	End of Medium
26	1A	032	Substitute
27	1B	033	Escape
28	1C	034	File Separator
29	1D	035	Group Separator
30	1E	036	Record Separator
31	1F	037	Unit Separator

Dec	Hex	Oct	HTML	Chr
32	20	040	 	Space
33	21	041	!	!
34	22	042	"	"
35	23	043	#	#
36	24	044	$	$
37	25	045	%	%
38	26	046	&	&
39	27	047	'	'
40	28	050	(	(
41	29	051	)	)
42	2A	052	*	*
43	2B	053	+	+
44	2C	054	,	,
45	2D	055	-	-
46	2E	056	.	.
47	2F	057	/	/
48	30	060	0	0
49	31	061	1	1
50	32	062	2	2
51	33	063	3	3
52	34	064	4	4
53	35	065	5	5
54	36	066	6	6
55	37	067	7	7
56	38	070	8	8
57	39	071	9	9
58	3A	072	:	:
59	3B	073	;	;
60	3C	074	<	<
61	3D	075	=	=
62	3E	076	>	>
63	3F	077	?	?

Dec	Hex	Oct	HTML	Chr
64	40	100	@	@
65	41	101	A	A
66	42	102	B	B
67	43	103	C	C
68	44	104	D	D
69	45	105	E	E
70	46	106	F	F
71	47	107	G	G
72	48	110	H	H
73	49	111	I	I
74	4A	112	J	J
75	4B	113	K	K
76	4C	114	L	L
77	4D	115	M	M
78	4E	116	N	N
79	4F	117	O	O
80	50	120	P	P
81	51	121	Q	Q
82	52	122	R	R
83	53	123	S	S
84	54	124	T	T
85	55	125	U	U
86	56	126	V	V
87	57	127	W	W
88	58	130	X	X
89	59	131	Y	Y
90	5A	132	Z	Z
91	5B	133	[	[
92	5C	134	\	\
93	5D	135	]	]
94	5E	136	^	^
95	5F	137	_	_

Dec	Hex	Oct	HTML	Chr
96	60	140	`	`
97	61	141	a	a
98	62	142	b	b
99	63	143	c	c
100	64	144	d	d
101	65	145	e	e
102	66	146	f	f
103	67	147	g	g
104	68	150	h	h
105	69	151	i	i
106	6A	152	j	j
107	6B	153	k	k
108	6C	154	l	l
109	6D	155	m	m
110	6E	156	n	n
111	6F	157	o	o
112	70	160	p	p
113	71	161	q	q
114	72	162	r	r
115	73	163	s	s
116	74	164	t	t
117	75	165	u	u
118	76	166	v	v
119	77	167	w	w
120	78	170	x	x
121	79	171	y	y
122	7A	172	z	z
123	7B	173	{	{
124	7C	174	|	|
125	7D	175	}	}
126	7E	176	~	~
127	7F	177	&#127;	Del

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Activity: Binary to Text

You do: translate the following binary into ASCII text. We've already translated binary to decimal for you.

01011001 = 89

01100001 = 97

01111001 = 121

Dec	Hex	Oct	Chr	Dec	Hex	Oct	HTML	Chr	Dec	Hex	Oct	HTML	Chr	Dec	Hex	Oct	HTML	Chr
0	0	000	NULL	32	20	040	 	Space	64	40	100	@	@	96	60	140	`	`
1	1	001	Start of Header	33	21	041	!	!	65	41	101	A	A	97	61	141	a	a
2	2	002	Start of Text	34	22	042	"	"	66	42	102	B	B	98	62	142	b	b
3	3	003	End of Text	35	23	043	#	#	67	43	103	C	C	99	63	143	c	c
4	4	004	End of Transmission	36	24	044	$	$	68	44	104	D	D	100	64	144	d	d
5	5	005	Enquiry	37	25	045	%	%	69	45	105	E	E	101	65	145	e	e
6	6	006	Acknowledgment	38	26	046	&	&	70	46	106	F	F	102	66	146	f	f
7	7	007	Bell	39	27	047	'	'	71	47	107	G	G	103	67	147	g	g
8	8	010	Backspace	40	28	050	(	(	72	48	110	H	H	104	68	150	h	h
9	9	011	Horizontal Tab	41	29	051	)	)	73	49	111	I	I	105	69	151	i	i
10	A	012	Line feed	42	2A	052	*	*	74	4A	112	J	J	106	6A	152	j	j
11	B	013	Vertical Tab	43	2B	053	+	+	75	4B	113	K	K	107	6B	153	k	k
12	C	014	Form feed	44	2C	054	,	,	76	4C	114	L	L	108	6C	154	l	l
13	D	015	Carriage return	45	2D	055	-	-	77	4D	115	M	M	109	6D	155	m	m
14	E	016	Shift Out	46	2E	056	.	.	78	4E	116	N	N	110	6E	156	n	n
15	F	017	Shift In	47	2F	057	/	/	79	4F	117	O	O	111	6F	157	o	o
16	10	020	Data Link Escape	48	30	060	0	0	80	50	120	P	P	112	70	160	p	p
17	11	021	Device Control 1	49	31	061	1	1	81	51	121	Q	Q	113	71	161	q	q
18	12	022	Device Control 2	50	32	062	2	2	82	52	122	R	R	114	72	162	r	r
19	13	023	Device Control 3	51	33	063	3	3	83	53	123	S	S	115	73	163	s	s
20	14	024	Device Control 4	52	34	064	4	4	84	54	124	T	T	116	74	164	t	t
21	15	025	Negative Ack.	53	35	065	5	5	85	55	125	U	U	117	75	165	u	u
22	16	026	Synchronous idle	54	36	066	6	6	86	56	126	V	V	118	76	166	v	v
23	17	027	End of Trans. Block	55	37	067	7	7	87	57	127	W	W	119	77	167	w	w
24	18	030	Cancel	56	38	070	8	8	88	58	130	X	X	120	78	170	x	x
25	19	031	End of Medium	57	39	071	9	9	89	59	131	Y	Y	121	79	171	y	y
26	1A	032	Substitute	58	3A	072	:	:	90	5A	132	Z	Z	122	7A	172	z	z
27	1B	033	Escape	59	3B	073	;	;	91	5B	133	[	[	123	7B	173	{	{
28	1C	034	File Separator	60	3C	074	<	<	92	5C	134	\	\	124	7C	174	|	|
29	1D	035	Group Separator	61	3D	075	=	=	93	5D	135	]	]	125	7D	175	}	}
30	1E	036	Record Separator	62	3E	076	>	>	94	5E	136	^	^	126	7E	176	~	~
31	1F	037	Unit Separator	63	3F	077	?	?	95	5F	137	_	_	127	7F	177	&#127;	Del

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Activity Answer

01011001 = 89

Y

01100001 = 97

a

01111001 = 121

y

Answer = "yay"

Dec	Hex	Oct	Chr		Dec	Hex	Oct	HTML	Chr		Dec	Hex	Oct	HTML	Chr		Dec	Hex	Oct	HTML	Chr
0	0	000	NULL		32	20	040	 	Space		64	40	100	@	@		96	60	140	`	`
1	1	001	Start of Header		33	21	041	!	!		65	41	101	A	A		97	61	141	a	a
2	2	002	Start of Text		34	22	042	"	"		66	42	102	B	B		98	62	142	b	b
3	3	003	End of Text		35	23	043	#	#		67	43	103	C	C		99	63	143	c	c
4	4	004	End of Transmission		36	24	044	$	$		68	44	104	D	D		100	64	144	d	d
5	5	005	Enquiry		37	25	045	%	%		69	45	105	E	E		101	65	145	e	e
6	6	006	Acknowledgment		38	26	046	&	&		70	46	106	F	F		102	66	146	f	f
7	7	007	Bell		39	27	047	'	'		71	47	107	G	G		103	67	147	g	g
8	8	010	Backspace		40	28	050	(	(		72	48	110	H	H		104	68	150	h	h
9	9	011	Horizontal Tab		41	29	051	)	)		73	49	111	I	I		105	69	151	i	i
10	A	012	Line feed		42	2A	052	*	*		74	4A	112	J	J		106	6A	152	j	j
11	B	013	Vertical Tab		43	2B	053	+	+		75	4B	113	K	K		107	6B	153	k	k
12	C	014	Form feed		44	2C	054	,	,		76	4C	114	L	L		108	6C	154	l	l
13	D	015	Carriage return		45	2D	055	-	-		77	4D	115	M	M		109	6D	155	m	m
14	E	016	Shift Out		46	2E	056	.	.		78	4E	116	N	N		110	6E	156	n	n
15	F	017	Shift In		47	2F	057	/	/		79	4F	117	O	O		111	6F	157	o	o
16	10	020	Data Link Escape		48	30	060	0	0		80	50	120	P	P		112	70	160	p	p
17	11	021	Device Control 1		49	31	061	1	1		81	51	121	Q	Q		113	71	161	q	q
18	12	022	Device Control 2		50	32	062	2	2		82	52	122	R	R		114	72	162	r	r
19	13	023	Device Control 3		51	33	063	3	3		83	53	123	S	S		115	73	163	s	s
20	14	024	Device Control 4		52	34	064	4	4		84	54	124	T	T		116	74	164	t	t
21	15	025	Negative Ack.		53	35	065	5	5		85	55	125	U	U		117	75	165	u	u
22	16	026	Synchronous idle		54	36	066	6	6		86	56	126	V	V		118	76	166	v	v
23	17	027	End of Trans. Block		55	37	067	7	7		87	57	127	W	W		119	77	167	w	w
24	18	030	Cancel		56	38	070	8	8		88	58	130	X	X		120	78	170	x	x
25	19	031	End of Medium		57	39	071	9	9		89	59	131	Y	Y		121	79	171	y	y
26	1A	032	Substitute		58	3A	072	:	:		90	5A	132	Z	Z		122	7A	172	z	z
27	1B	033	Escape		59	3B	073	;	;		91	5B	133	[	[		123	7B	173	{	{
28	1C	034	File Separator		60	3C	074	<	<		92	5C	134	\	\		124	7C	174	|		
29	1D	035	Group Separator		61	3D	075	=	=		93	5D	135	]	]		125	7D	175	}	}
30	1E	036	Record Separator		62	3E	076	>	>		94	5E	136	^	^		126	7E	176	~	~
31	1F	037	Unit Separator		63	3F	077	?	?		95	5F	137	_	_		127	7F	177	&#127;	Del

asciichars.com

For More Characters, Use Unicode

There are plenty of characters that aren't available in ASCII (characters from non-English languages, advanced symbols, emoji...) due to the limited size.
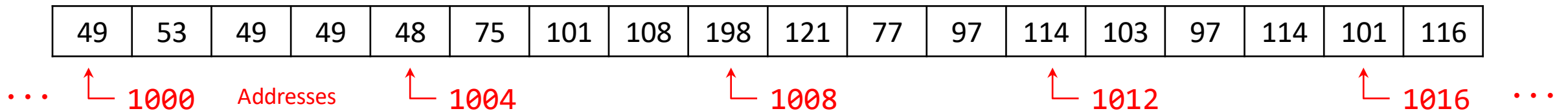
The Unicode system represents every character that can be typed into a computer. It uses up to 5 bytes, which can represent up to 1 trillion characters! Find all the Unicode characters here: www.unicode-table.com

The Unicode system is also **actively under development**. The Unicode Consortium regularly updates the standard to add new types of characters and emoji.

Computer Memory is Stored as Binary

Your computer keeps track of saved data and all the information it needs to run in its **memory**, which is represented as binary. You can think about your computer's memory as a really long list of bits, where each bit can be set to 0 or 1. But usually we think in terms of bytes, groups of 8 bits.

Every byte in your computer has an **address**, which the computer uses to look up its value.

49	53	49	49	48	75	101	108	198	121	77	97	114	103	97	114	101	116

· · · └ 1000   Addresses   └ 1004   └ 1008   └ 1012   └ 1016   · · ·

Binary Values Depend on Interpretation

When you open a file on your computer, the application goes to the appropriate address, reads the associated binary, and **interprets** the binary values based on the file encoding it expects. That interpretation depends on the **application** you use when opening the file, and the **filetype**.

You can attempt to open **any file** using **any program**, if you convince your computer to let you try. Some programs may crash, and others will show nonsense because the binary isn't being interpreted correctly.

Example: try changing a .docx filetype to .txt, then open it in a plain text editor. .docx files have extra encoding, whereas .txt files use plain ASCII.

We Use Lots of Bytes!

In modern computing, we use a **lot** of bytes to represent information.

Smartphone Memory: 64 gigabytes = 64 **billion** bytes

Google databases: Over 100 million gigabytes = 100 **quadrillion** bytes!

CMU Wifi: 15 **million** bytes per second

Learning Objectives

- Understand how different **number systems** can represent the same information

- Translate **binary numbers** to decimal, and vice versa

- Interpret binary numbers as abstracted types, including **colors** and **text**